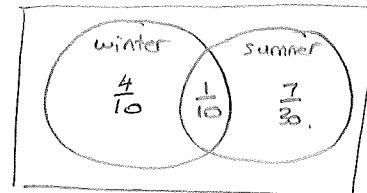


CIMT Stats pl3 EX 1 C.

- $P(\text{winter sport}) = \frac{1}{2}$
- $P(\text{summer sport}) = \frac{1}{3}$.
- $P(\text{both winter + summer sports}) = \frac{1}{10}$



$$\frac{1}{2} - \frac{1}{10} = \frac{4}{10}$$

$$\frac{1}{3} - \frac{1}{10} = \frac{10}{30} - \frac{3}{30} = \frac{7}{30}$$

$$\begin{aligned}
 P(\text{sporty person selected}) &= \frac{4}{10} + \frac{1}{10} + \frac{7}{30} \\
 &= \frac{5}{10} + \frac{7}{30} \\
 &= \frac{15}{30} + \frac{7}{30} \\
 &= \frac{22}{30} \\
 &= \underline{\underline{\frac{11}{15}}}.
 \end{aligned}$$

- $P(A \text{ wins prize}) = \frac{1}{3}$

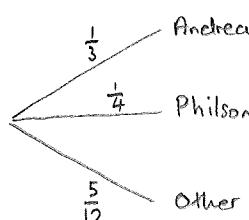
$$P(\text{Philson wins prize}) = \frac{1}{4}$$

only one person can win the prize

\Rightarrow events are mutually exclusive

$$P(\text{one will win it}) = \frac{1}{3} + \frac{1}{4}$$

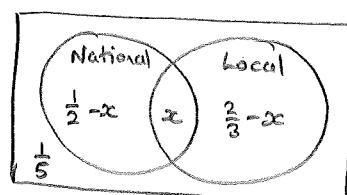
$$= \underline{\underline{\frac{7}{12}}}.$$



- $P(\text{no newspapers}) = \frac{1}{5}$

$$P(\text{national paper}) = \frac{1}{2}$$

$$P(\text{local paper}) = \frac{2}{3}$$



If $P(\text{no newspapers}) = \frac{1}{5}$

$$\Rightarrow P(\text{at least one newspaper}) = \frac{4}{5}$$

$$\therefore (\frac{1}{2} - x) + x + (\frac{2}{3} - x) = \frac{4}{5}$$

$$\Rightarrow \frac{3}{6} + \frac{4}{6} - x = \frac{4}{5}$$

$$\Rightarrow x = \frac{7}{6} - \frac{4}{5} = \frac{35-24}{30} = \underline{\underline{\frac{11}{30}}}$$

$$\therefore P(\text{both newspapers}) = \underline{\underline{\frac{11}{30}}}.$$

Ex 1 C cont.

4. exhaustive $\Rightarrow P(X \cup Y) = 1$.

mutually exclusive $\Rightarrow P(X \cap Y) = 0$.

a) $P(A \cap D)$

$= P(\text{total is } 3 \text{ and red die is multiple of } 3)$

$= 0$ as these cannot happen at the same time

$\hookrightarrow A \& D$ are mutually exclusive.

A : total is 3

	1	2	3	4	5	6
R	1	✓				
	2	✓				
	3					
	4					
	5					
	6					

$$P(A) = \frac{2}{36}$$

D: 1 2 3 4 5 6

	1	2	3	4	5	6
R	1	✓	✓	✓	✓	✓
	2					
	3					
	4					
	5					
	6					

$$P(D) = \frac{12}{36}$$

b) $P(C \cap E)$

$= P(\text{total is } \leq 9 \text{ and total } \geq 11)$

$= 0$ as these cannot happen at the same time

$\hookrightarrow C \& E$ are mutually exclusive.

c) $P(A \cap B)$

$= P(\text{total is } 3 \text{ and red is a multiple of } 2)$

$$= \frac{1}{36}$$

$\neq 0 \text{ or } 1$

$\hookrightarrow A \text{ and } B$ are neither exhaustive or mutually exclusive.

d) $P(C \cup F)$

$$P(C \cap F) = 0$$

$= P(\text{total } \leq 9 \text{ or total is } \geq 10)$

$$= 1$$

$\hookrightarrow C \text{ and } F$ are exhaustive and mutually exclusive

e) $P(B \cap D)$

$= P(\text{red is multiple of } 2 \text{ and red is a multiple of } 3)$

$$= \frac{1}{6}$$

$\neq 0$

$$P(B \cup D) = \frac{4}{6} \neq 1$$

$\hookrightarrow B \text{ and } D$ are neither exhaustive or mutually exclusive.

f) $P(\text{total is } 3 \text{ and total } \geq 10) = 0$

$\hookrightarrow A \text{ and } E$ are mutually exclusive.