

CIMT Statistics p182. Example.

$$n = 100$$

sample mean,  $\bar{x} = 180\text{cm}$

known population variance,  $\sigma^2 = 49$

let  $X = \text{height of man}$

$$E(X) = \mu$$

$$\text{Var}(X) = 49$$

by CLT (as  $n$  is large),  $\bar{X} \sim N(\mu, \frac{\sigma^2}{n})$

so a 95% CI for  $\mu$  is  $\bar{x} \pm z_{0.025} \sqrt{\frac{\sigma^2}{n}}$

$$= 180 \pm 1.95996 \sqrt{\frac{49}{100}}$$

$$= (178.628, 181.372)$$

$$= (178.6, 181.4) \text{ to 1 dp.}$$

$$z_{0.025} = \text{invNorm}(0.975) = 1.95996$$

$$\text{from } 180 + \{-1, 1\} \text{ invNorm}(0.975) \sqrt{\frac{49}{100}}$$

check with TI-Nspire

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And read note on p183 that starts "It should be noted..."