

P207 Ex 11A Qn 1

| Score | 1  | 2  | 3  | 4  | Total. |
|-------|----|----|----|----|--------|
| $f_o$ | 12 | 15 | 19 | 22 | 68     |
| $f_e$ | 17 | 17 | 17 | 17 | 68     |

$H_0$ : the observed data fits the discrete uniform distribution,  $U(4)$

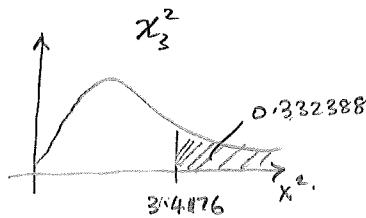
$H_1$ : data does not fit  $U(4)$

Assume  $H_0$  to be true       $\alpha = 5\%$ .  
one tail test

$$\chi^2 = \sum \left( \frac{f_o - f_e}{f_e} \right)^2 = 3.41176$$

$$df = 3.$$

$$P(\chi^2 > 3.41176) = 0.332388$$



Hence as  $0.33 > 0.05$ , based on the 68 trials, we do not

have evidence to reject  $H_0$  and we conclude that the observed data fits a  $U(4)$  distribution, and so the die is fair.

Ex II A no. 2.

| Score | 1  | 2  | 3  | 4  | 5  | 6   | Total |
|-------|----|----|----|----|----|-----|-------|
| $f_0$ | 17 | 20 | 29 | 20 | 18 | 16  | 120.  |
| $f_e$ | 20 | 20 | 20 | 20 | 20 | 20. |       |

$H_0$ : Die is fair & fits discrete uniform distribution,  $U(6)$

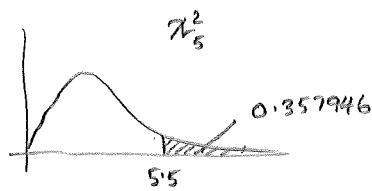
$H_1$ : Die is not uniformly distributed

Assume  $H_0$  to be true.

$\alpha = 5\%$ , 1 tail test,  $df = 5$ .

$$\chi^2 = \sum \frac{(f_0 - f_e)^2}{f_e} = 5.5$$

$$P(\chi^2 > 5.5) = 0.357946$$



as  $0.35 > 0.05$ , we do not have evidence to reject  $H_0$  and we conclude that the die is not biased, as it follows a  $U(6)$  distribution

Ex 11 A no. 3

| Day            | M   | Tu  | W   | Th  | F.  |
|----------------|-----|-----|-----|-----|-----|
| A <sub>o</sub> | 125 | 88  | 85  | 94  | 108 |
| F <sub>e</sub> | 100 | 100 | 100 | 100 | 100 |

$H_0$ : absences independent of day (distributed as discrete uniform  $U(5)$ )

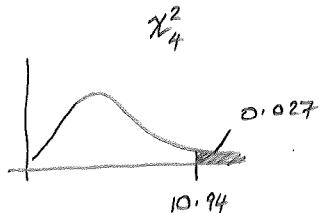
$H_1$ : absences not independent of day, (as not uniformly distributed)

Assume  $H_0$  to be true.

$\alpha = 5\%$ , one-tail test,  $df = 4$

$$\chi^2 = 10.94$$

$$P(\chi^2 > 10.94) = 0.027247$$



as  $0.027 < 0.05$ , we have evidence to reject  $H_0$ , and so the absences are not  $U(5)$  distributed.

Hence, on the basis of this observed data, there is evidence that the observed and

expected frequencies are significantly different and that the absences are not independent of the day (we conjecture that there is a "I don't like Monday"

phenomenon, courtesy of Bob Geldof and the Boomtown Rats).